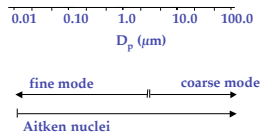


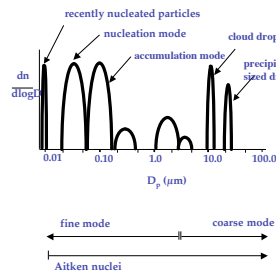
Particle Sizes

- range of particle sizes is approximately from 1 nm to 1 mm in diameter
- range of approximately 6 orders of magnitude
- concentrations at each of these sizes also vary



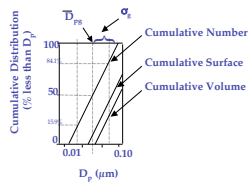
Size Distribution Modes

- modes of aerosol are distinguished by
 - size
 - sources
 - behavior

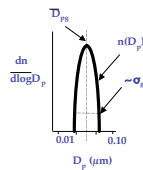


Log-Normal Number Distributions

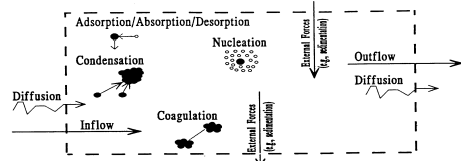
- Cumulative



- Differential

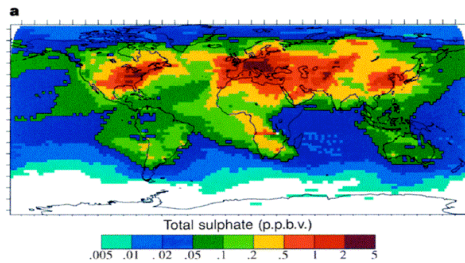


Microphysics



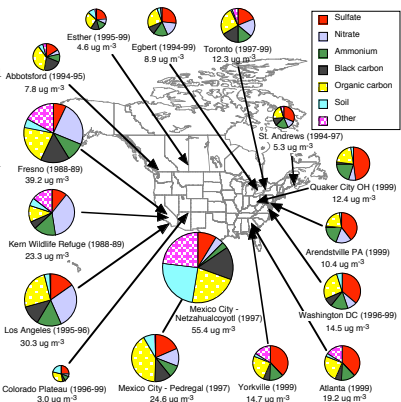
- Aerosol includes both particles and vapor
- Number, area, volume, mass vary nonlinearly
- Deposition velocity depends on size (nano, micro, milli)
- Scavenging, coalescence, activation and condensation change the size distribution

Global Aerosol Distribution



Capaldo et al., *Nature*, 1999

- Regional variations in aerosol mass and composition [NARSTO, 2002]



ROAST Reviews

- Review comments due to editor: Nov. 6
 - Reviews are completed by individuals not groups.
 - Reviewer's name should **not** appear in review.
 - Reviewer's name should be in filename.
 - "GroupAp1v1reviewLASTNAME.pdf"
- <http://www.elsevier.com/wps/find/editorsinfo.editors/ebu/issue5a>

Homework Ch. 5 Prob. 3

$$r^* = \sqrt{\frac{3b}{a}}$$

$$S^* = 1 + \sqrt{\frac{4a^3}{27b}}$$

$$a = 2\sigma_{iv}/(\rho_l R_v T)$$

$$b = 3rM_v \frac{m_{sol}}{4\pi M_{sol} \rho_l}$$

rho_l	1000 kg/m3	
sigma_iv	0.075015 N/m	
Rv	461.478686 J/K/KG	
T	280 K	
I	2	
M_v	18.016 g/mol	
M_sol	132.1 g/mol	
m_sol	1.00E-18 KG	
a	1.1611E-09 m	a=2sigma/(rho*Rv*T)
b	6.5117E-23 m3	b=3rMv*m_sol/(4pi*M_sol*rho)
r*	4.1038E-07 m	r*=sqrt(3b/a)
S*	1.00188713	S*=1+sqrt(4a^3/27b)

Eqn. 5.7

Example Ch. 5 Prob. 7

Curry and Webster, p. 158, Problem 7a-c

7. An analytic expression of the following form has been used to describe drop size spectra:

$$n(r) = Ar^2 \exp(-Br)$$

where A and B are parameters. For a drop size spectrum represented by this relationship, determine the following:

a) the total drop concentration per volume of air:

$$N = \int_0^{\infty} n(r) dr$$

b) the mean drop radius:

$$\bar{r} = \frac{1}{N} \int_0^{\infty} r n(r) dr$$

c) the coefficients A and B for $N = 200 \text{ cm}^{-3}$ and $\bar{r} = 10 \mu\text{m}$;

Integral Tables (521), CRC 1986 p. 330

$$\int x^m e^{ax} dx = \frac{x^m e^{ax}}{a} - \frac{m}{a} \int x^{m-1} e^{ax} dx = e^{ax} \sum_{r=0}^m (-1)^r \frac{m! x^{m-r}}{(m-r)! a^{r+1}}$$

Example Ch. 5 Prob. 7

a) the total drop concentration per volume of air:

$$n(r) = Ar^2 \exp(-Br)$$

$$N = \int_0^{\infty} n(r) dr$$

$$N = \int_0^{\infty} Ar^2 e^{-Br} dr$$

$$= A \frac{e^{-Br}}{-B} \left(r^2 - \frac{2}{B} (-Br - 1) \right) \Big|_0^{\infty}$$

$$= 0 - \left[-\frac{A}{B} \left(\frac{2}{B^2} \right) \right]$$

$$= \frac{2A}{B^3}$$

Integral Tables (521)
CRC 1986 p. 330

$$\int x^m e^{ax} dx = e^{ax} \sum_{r=0}^m (-1)^r \frac{m! x^{m-r}}{(m-r)! a^{r+1}}$$

$$\int x^2 e^{ax} dx = \frac{e^{ax}}{a} \left(x^2 - \frac{2}{a} (ax - 1) \right)$$

Example Ch. 5 Prob. 7

b) the mean drop radius:

$$\bar{r} = \frac{1}{N} \int_0^{\infty} r n(r) dr$$

$$n(r) = Ar^2 \exp(-Br)$$

$$\bar{r} = \frac{1}{N} \int_0^{\infty} Ar^3 e^{-Br} dr$$

$$= \frac{A}{N} \left(\frac{e^{-Br}}{-B} \right) \left(r^3 + \frac{3r^2}{B} - \frac{6}{B^2} (-Br - 1) \right) \Big|_0^{\infty}$$

$$= 0 - \left[-\frac{A}{BN} \left(\frac{6}{B^3} \right) \right]$$

$$= \frac{3}{B}$$

Integral Tables (521)
CRC 1986 p. 330

$$\int x^m e^{ax} dx = e^{ax} \sum_{r=0}^m (-1)^r \frac{m! x^{m-r}}{(m-r)! a^{r+1}}$$

$$\int x^3 e^{ax} dx = \frac{e^{ax}}{a} \left(x^3 - \frac{3x^2}{a} + \frac{6}{a^2} (ax - 1) \right)$$

Example Ch. 5 Prob. 7

c) the coefficients A and B for $N = 200 \text{ cm}^{-3}$ and $\bar{r} = 10 \mu\text{m}$;

$$\bar{r} = \frac{3}{B} = 10 \times 10^{-6}$$

$$B = 3 \times 10^5$$

$$N = \frac{2A}{B^3} = 200 \times 10^6$$

$$A = 2.7 \times 10^{24}$$

Example Ch. 5 Prob. 7

d) the liquid water mixing ratio, w_l :

$$n(r) = Ar^2 \exp(-Br)$$

$$w_l = \frac{\rho_l}{\rho_a} \frac{4}{3} \rho \int_0^\infty r n(r) dr$$

Integral Tables (521)
CRC 1986 p. 330

$$\int x^m e^{ax} dx = e^{ax} \sum_{r=0}^m (-1)^r \frac{m! x^{m-r}}{(m-r)! a^{r+1}}$$

$$= 120 e^{ax} \left(\frac{x^5}{120a} - \frac{x^4}{24a^2} + \frac{x^3}{6a^3} - \frac{x^2}{2a^4} + \frac{x}{a^5} - \frac{1}{a^6} \right)$$

$$w_l = \left(\frac{4\pi A \rho_l}{3\rho_a} \right) \int r^5 e^{-Br} dr$$

$$= \left(\frac{4\pi A \rho_l}{3\rho_a} \right) 120 e^{-Br} \left(-\frac{r^5}{120B} + \frac{r^4}{24B^2} - \frac{r^3}{6B^3} + \frac{r^2}{2B^4} - \frac{r}{B^5} + \frac{1}{B^6} \right) \Big|_0^\infty$$

$$= \left(\frac{4\pi A \rho_l}{3\rho_a} \right) \left(0 - \frac{-120}{B^6} \right) = \left(\frac{160\pi A \rho_l}{B^6 \rho_a} \right)$$

Cloud in a Jar Demonstration

Adiabatic Processes
EXPANSION CLOUD CHAMBER

- A rubber bulb fits into the top of a gallon jug, which contains a small amount of water.
- Slosh the water around in the jug to saturate the air with water vapor.
- Drop a lighted match into the jug and put the bulb on the top.
- Squeeze and release the bulb rapidly to create the "cloud".
- A 5-gallon jug is also available. Use your lungs to create the necessary under-pressure. (The bulb is too small.)

http://groups.physics.umn.edu/demo/old_page/demo_gifs/4B70_20.GIF

Lecture Ch. 6a

100%. For simplicity, we assume here that clouds form in the atmosphere when the water vapor reaches its saturation value and $\mathcal{H}=100\%$.

- Saturation of moist air
- Relationship between humidity and dewpoint
 - Clausius-Clapeyron equation
- Dewpoint
 - Temperature
 - Depression
- Isobaric cooling

Curry and Webster, Ch. 6
For Tuesday: Read Ch. 7

How does saturation occur?

- By increasing water vapor
 - Evaporation of water at surface
 - Evaporation of falling rain
- By cooling
 - Isobaric
 - Radiative cooling of rising air
- By mixing of two unsaturated air parcels

Curry and Webster, Ch. 6

Saturation of Moist Air

- Dew point temperature

The temperature at which saturation is reached in an isobaric cooling process is the *dew-point temperature*, which is illustrated in Figure 6.1a. The dew-point temperature, denoted by T_D , can be defined by

$$e = e_s(T_D) \tag{6.14}$$

or equivalently by

$$w_s = w_s(T_D) \tag{6.15}$$

Curry and Webster, Ch. 6

Figure 6.1 a) Relationship between temperature and vapor pressure in an isobaric cooling process. Air initially at temperature T_1 (point 1) is cooled isobarically until it reaches saturation (point 2). The temperature at point 2 defines the dew-point temperature, T_D . b) Air at T_1 (point 1) cools isobarically until it reaches saturation. If the saturation is reached with respect to ice (point 2), the temperature is called the frost point, T_f .